

# Interpretation of Low Dimensional Neural Network Bottleneck Features in Terms of Human Perception and Production

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## What This Work is About

Analysis of very low-dimensional bottleneck features.

- spatial representation of **vowels** is **very close to  $F_1:F_2$** ;
- **consonants** are analysed in the **same framework**;
- neural networks seem to derive representations specific to particular phonetic categories —
- properties similar to those used by **human perception**.

## Bottleneck Features (BNFs) and Models of Speech

Speech suggested to lie on low-dimensional manifolds (e.g. [1]).

- for **Vowels**: 81.6% acoustic variation is explained by 3 dimensions (94.0% with 5) (*Pols et al.* [2]) — cf formants  $F_1 - F_3$ ;
- for **Fricatives**: 95% by 2 dimensions (*Choo et al.* [3]).

Segmental and Continuous-State HMM models for ASR

- aim to be faithful to the nature and dynamics of speech,
- but had difficulty adequately modelling (e.g.) the all variability in natural low-dimensional representations such as formants.
- **9d Bottleneck features found to perform well in CS-HMMs** [4]:

| Network Dim./Layer | Autoencoder |      | MLP  |      | DBN  |      |
|--------------------|-------------|------|------|------|------|------|
|                    | 3d/3        | 9d/3 | 3d/3 | 9d/3 | 3d/4 | 9d/4 |
| all phones         | 64.8        | 60.8 | 47.8 | 37.9 | 43.8 | 35.2 |
| voiced only        | 72.7        | 65.6 | 50.5 | 43.8 | 47.7 | 40.3 |
| unvoiced           | 40.5        | 37.7 | 30.2 | 20.6 | 26.6 | 19.9 |

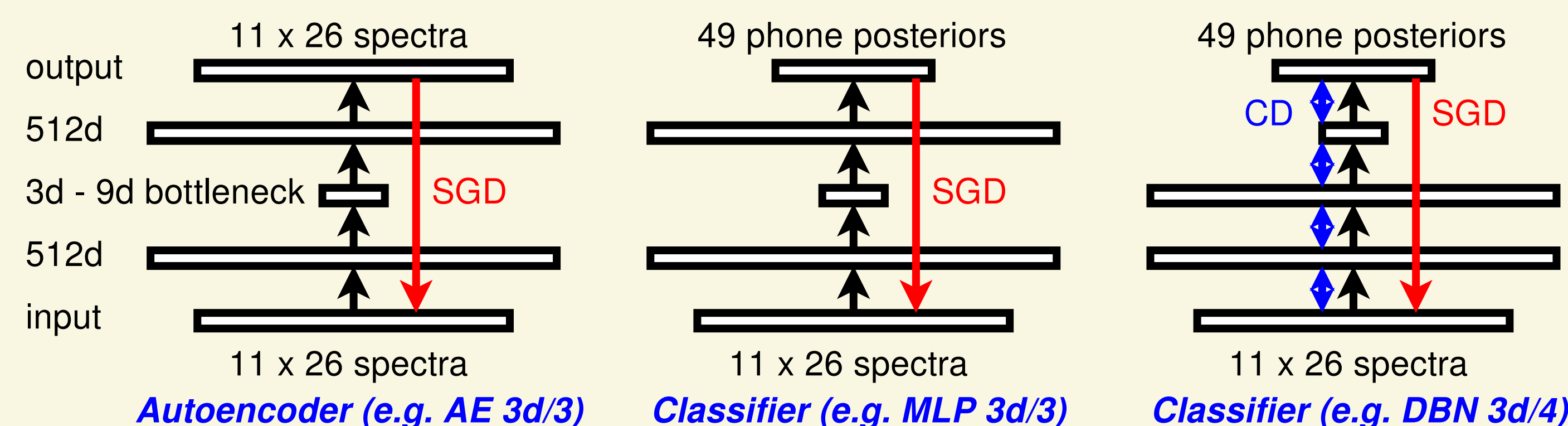
CS-HMM phone recognition % Error using bottleneck features (BNFs).

**But what do the BNF features represent?**  
**Can they be related to human perception or production?**

## Bottleneck Networks

Bottleneck Features (BNFs) from 3 types of networks (from TIMIT).

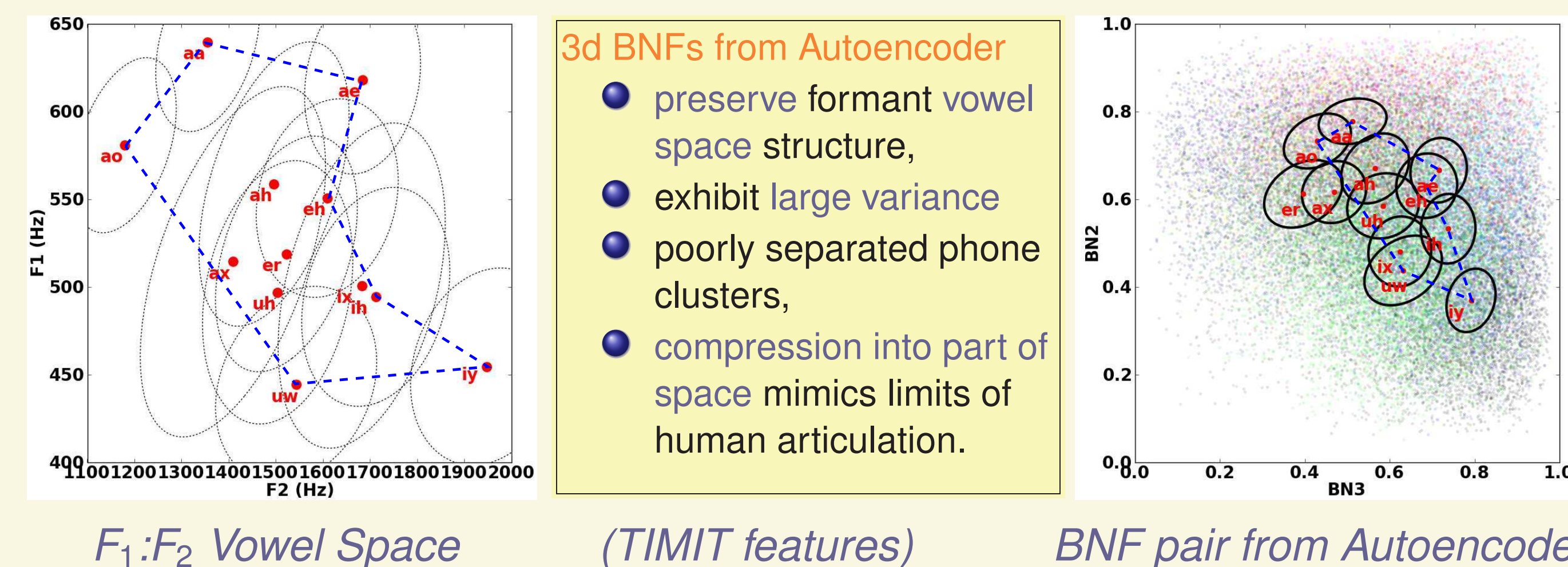
- 1 Autoencoders: reconstruct input.
- 2 MLP Classifiers (SGD-trained): predict posteriors for 49 phones.
- 3 DBN Classifiers (CD pre-trained with SGD fine-tuning).



- **5 layers** (2d–9d bottleneck in layer 3 [e.g. ‘3d/3’] or 4 [‘3d/4’]).
- **Input**: 11 frames of 26-dimensional log Mel filterbanks.
- **Training**: SGD and/or CD using Theano, cross-entropy error.

## Vowels: Formants vs Autoencoder 3-dimensional BNFs

- 1 Pairwise plots of 3d BNFs in comparison with formants.
- 2 Visualisation and comparison using **metrics** to compare ‘shape’.

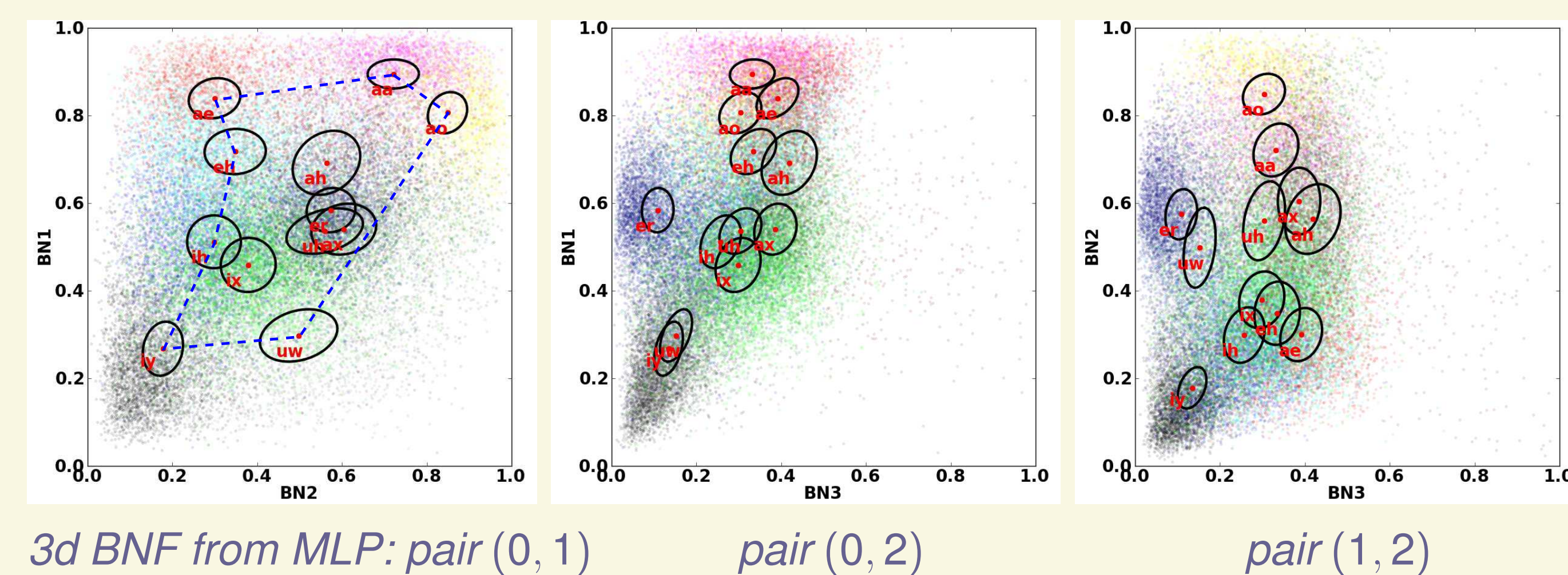


**Visualisation:** Features are represented spatially using 2d plots showing centroids and 0.5 s.d. of clusters of phone realisations (average feature between TIMIT boundaries) for a set of phones.

**Metrics:** Let  $X, Y$  be  $n \times 2$  matrices of points  $\mathbf{x}_i = (x_{i1}, x_{i2})$ ,  $\mathbf{y}_i = (y_{i1}, y_{i2})$  in two such plots. The shape  $\mathcal{D}_X$  described by connecting points  $\mathbf{x}_i$  is significant, but not its location or rotation.  $d_2(X, Y)$  is the Euclidean distance between points  $\mathbf{y}_i$  and the best-fit  $\hat{\mathbf{y}}_i$  found by affine transforming  $X$  towards  $Y$ ,

$$d_2(X, Y) = \frac{1}{n} \sum_{i=1}^n \sqrt{\sum_{j=1}^2 (y_{ij} - \hat{y}_{ij})^2}, \text{ for } \hat{Y} = AX, \text{ where } A = YX^{-1}.$$

## Vowels: Formants vs Classifier 3-dimensional BNFs



| Feature    | Pair   | Best Match                                         |       | Avg. Worst |       |
|------------|--------|----------------------------------------------------|-------|------------|-------|
|            |        | Formant                                            | $d_2$ | Formant    | $d_2$ |
| MLP 3d/3 a | (1, 3) | $F_1:F_2$                                          | 0.142 |            | 0.278 |
| MLP 3d/3 b | (1, 2) | $F_1:F_3$                                          | 0.195 |            | 0.336 |
| MLP 3d/3 c | (1, 2) | $F_1:F_2$                                          | 0.216 |            | 0.330 |
| MLP 3d/3 d | (1, 2) | $F_1:F_2$                                          | 0.119 |            | 0.339 |
| DBN 3d/4   | (2, 3) | $F_1:F_2$                                          | 0.176 |            | 0.363 |
| A/E 3d/3   | (2, 3) | $F_1:F_2$                                          | 0.192 |            | 0.388 |
| MFCC       |        | Inconclusive (mean $d_2 = 0.348$ , $d_s = 0.217$ ) |       |            |       |

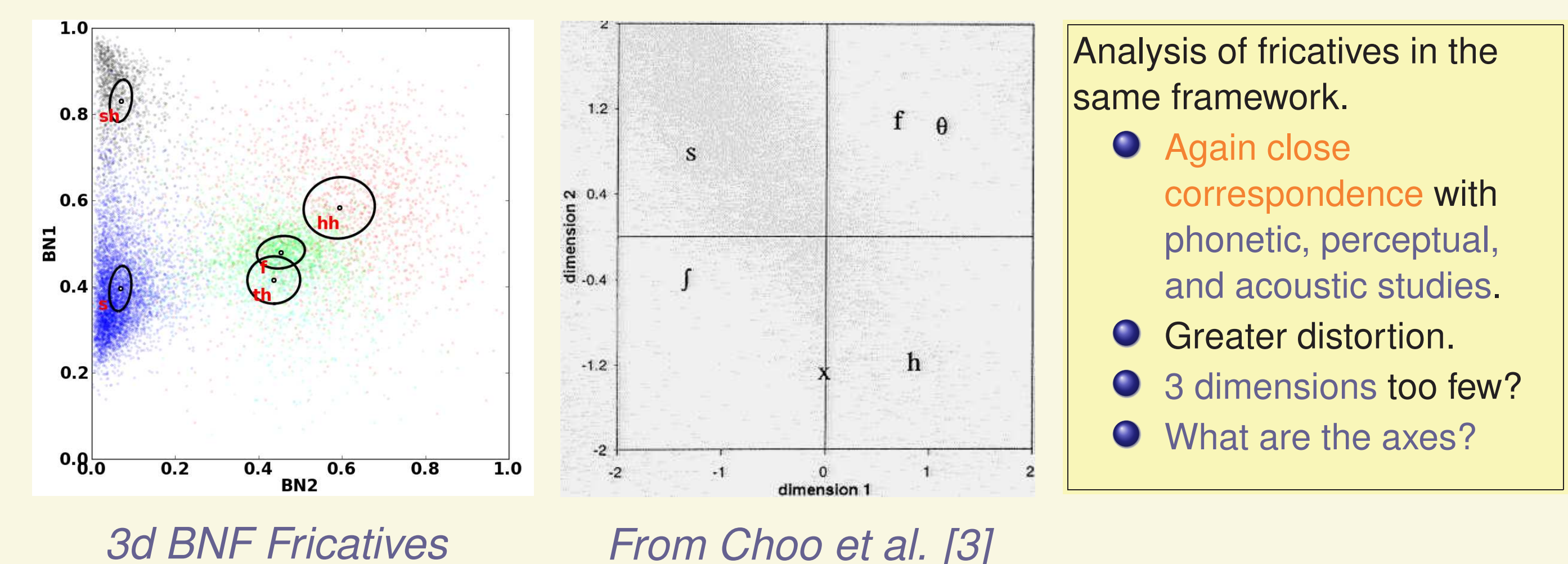
Distances between BNF and formant spaces.

### Summary:

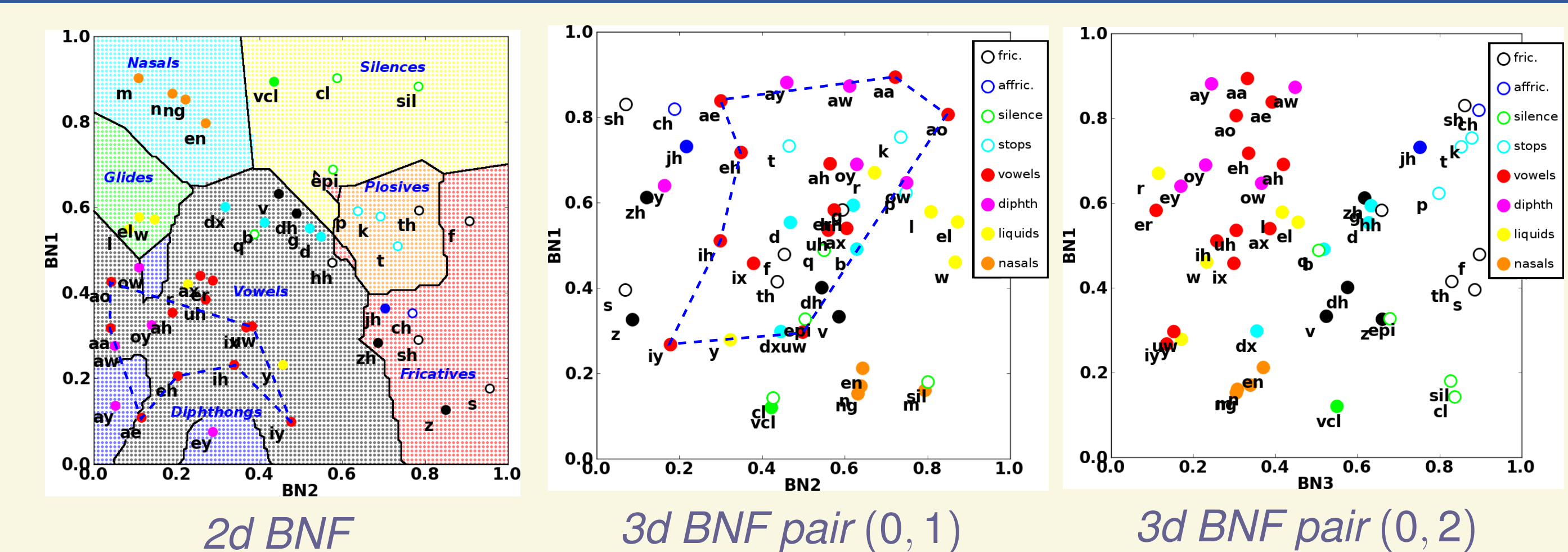
- One BNF pair always matches the vowel space.
- Reduced variance and increased cluster separation.
- 3<sup>rd</sup> dim. appears to relate to consonants or voicing.
- Metrics highlight a single anomaly – network reaches a different local optimum ( $F_1:F_3$ )?

**Robust and repeatable analysis without formant analysis.**

## Spatial Representations of Fricatives



## Unified Space for All Phones



### 2D BNF

- Space shows distinct regions used for each phonetic category.
- Divides voiced and unvoiced – voiced consonants on the border.
- Distorted vowel space structure – lost information.

### 3D BNF

- Co-location of phonetic categories in some dimensions.
- Some clustering according to place and manner of articulation.

## Discussion, Conclusions and Questions

**Robust and unified analysis framework for all phones.**

Unified space may be of benefit to speech scientists and therapists.

- Is it interpretable globally e.g. according to tongue position or acoustics (cf groups  $\{s/, /iy/, /z/\}$ ,  $\{zh/, /sh/\}$ ,  $\{w/, /l/, /ao/\}$ )?
- Can we gain insights into theories of perception?
- How would BNFs from RNNs better capture dynamics and other features of known perceptual importance?

## Selected References

- [1] G. Fant. “Acoustic Theory of Speech Production,” R. Jakobson and S. H. van Schooneveld, Eds., Mouton, 1970.
- [2] L. C. W. Pols, L. J. T. van der Kamp, and R. Plomp. “Perceptual and physical space of vowel sounds.” JASA, 46:456-467, 1969.
- [3] W. Choo and M. Huckvale, “Spatial Relationships in Fricative Perception”, *Speech, Hearing and Language: Work in Progress*, vol. 10, 1997.
- [4] P. Weber, L. Bai, S. M. Houghton, P. Jančovič, and M. J. Russell. “Progress on Phoneme Recognition with a Continuous-State HMM”. *ICASSP 2016*, Shanghai, pp. 5850-5854.